

# Energia geotermikoa

## 1. Eguzkia

$\phi$  (lekua)

$d$  (eguna)  $\rightarrow \bar{E}_t$   $\rightarrow$  Deribatzen ekwazioa  
(Spencer formula)

$\omega$  (ordua)

Ariketa) Kalkulatu Albazteko HSE

$$HSE = HSL - 4 \cdot (L_s - L_e) - E_t$$

$$4 \cdot (L_s - L_e) = 4 \cdot (0 - 1'52 \cdot \frac{10}{60}) = 4 \cdot (0 - 1'867) = -7'468 \text{ min}$$

$$HSE = 12:00:00 + 7'28'' + 2'54'' \rightarrow HSE = 12:10:22$$

## Eguzki-biltzaileak II

Adibidea

$$\phi = 39^\circ + \frac{42}{60}$$

$$\beta = 35^\circ$$

$$\psi = 0^\circ$$

$$J = 31 + 28 + 31 + 13 \begin{cases} \rightarrow d \\ \rightarrow C_{o,n} \end{cases}$$

### 3. Adibidea

$$\dot{Q}_{\text{eguzki}} = G_T \cdot A_c \cdot \alpha \cdot \tau$$

$$\dot{Q}_L = U_c A_c F (T_j - T_\infty)$$

$$\dot{Q}_u = \dot{m} \cdot c_p \cdot (T_o - T_i)$$

$$\eta = \frac{\dot{Q}_u}{G_T \cdot A_c}$$

$$A_c = 3 \text{ m}^2$$

$$G_T = 700 \text{ W/m}^2$$

$$\tau = 0.9$$

$$c_p = 4.18 \text{ kJ/kgK}$$

$$T = 30^\circ \text{C}$$

$$\varepsilon = 0.94$$

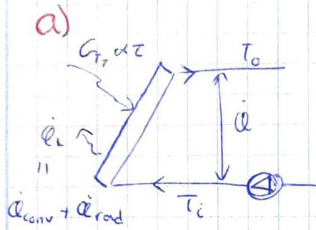
$$T_{\text{sky}} = -10^\circ \text{C}$$

$$\dot{Q}_{\text{rad}} = \varepsilon \sigma (T_s^4 - T_{\text{sky}}^4)$$

$$\dot{Q}_{\text{conv}} = h (T_s - T_\infty)$$

$$h = 10 \text{ W/m}^2\text{K}$$

$$T_\infty = 25^\circ \text{C}$$



$$\dot{Q}_{\text{eguzki}} = G_T \cdot A_c \cdot \tau \cdot \alpha = 0.9 \cdot 3 \cdot 700 = 1890 \text{ W}$$

$$\dot{Q}_L = \dot{Q}_{\text{conv}} + \dot{Q}_{\text{rad}}$$

$$\dot{Q}_{\text{conv}} = h \cdot A_c (T_s - T_\infty) = 10 \cdot 3 \cdot (30 - 25) = 150 \text{ W}$$

$$\dot{Q}_{\text{rad}} = \varepsilon \cdot \sigma \cdot A_c (T_s^4 - T_a^4) = 0.94 \cdot 5.67 \cdot 10^{-8} (303^4 - 263^4) = 583.6 \text{ W}$$

$$\dot{Q}_u = 1890 - 150 - 583.6 \rightarrow \dot{Q}_u = 1156.34 \text{ W}$$

$$\boxed{q_u = \frac{\dot{Q}_u}{A_c} = 385.1 \frac{\text{W}}{\text{m}^2}}$$

b)

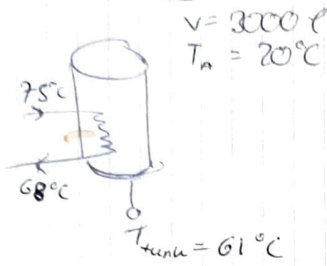
$$\dot{Q}_u = 1156.34 = \dot{m} \cdot c_p \cdot \Delta T \rightarrow \Delta T = \frac{\dot{Q}_u}{\dot{m} \cdot c_p} = \frac{1156.34}{0.01 \cdot 4180} \rightarrow \boxed{\Delta T = 27.67^\circ \text{C}}$$

c)

$$\eta = \frac{\dot{Q}_u}{A_c \cdot G_T} = \frac{1156.34}{3 \cdot 700} \rightarrow \boxed{\eta = 55.1\%}$$

# Biltegiak I

## 1. Adibidea



Karga

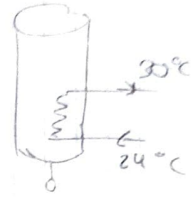
$$\Delta t = 40,60 = 2400 \text{ s}$$

$$\dot{m}_{\text{pin}} = 5 \text{ l/s}$$



Biltegiakote

$$\Delta t = 17,3600$$



Deskarga

$$\Delta t = 45,60 = 2700 \text{ s}$$

$$\dot{m}_{\text{pin}} = 5 \text{ l/s}$$

$Q_{\text{in}} ?$

$$Q_{\text{karga}} = \dot{m} \cdot C_p \cdot (T_{\text{in}} - T_{\text{out}}) \cdot \Delta t_1 = 5 \cdot 4,18 \cdot (75 - 68) \cdot 2400 \rightarrow Q_{\text{karga}} = 351120 \text{ kJ}$$

$T_{\text{ex}} ?$

$$Q_{\text{karga}} = Q_{\text{deskarga}} + Q_{\text{gulerak}}$$

$\eta_1, \eta_2, \eta_3 ?$

$$Q_{\text{deskarga}} = \dot{m} \cdot C_p \cdot (T_{\text{out}}^{\text{sk}} - T_{\text{in}}^{\text{sk}}) \cdot \Delta t_2 = 5 \cdot 4,18 \cdot (30 - 24) \cdot 2700 \rightarrow Q_{\text{deskarga}} = 339580 \text{ kJ}$$

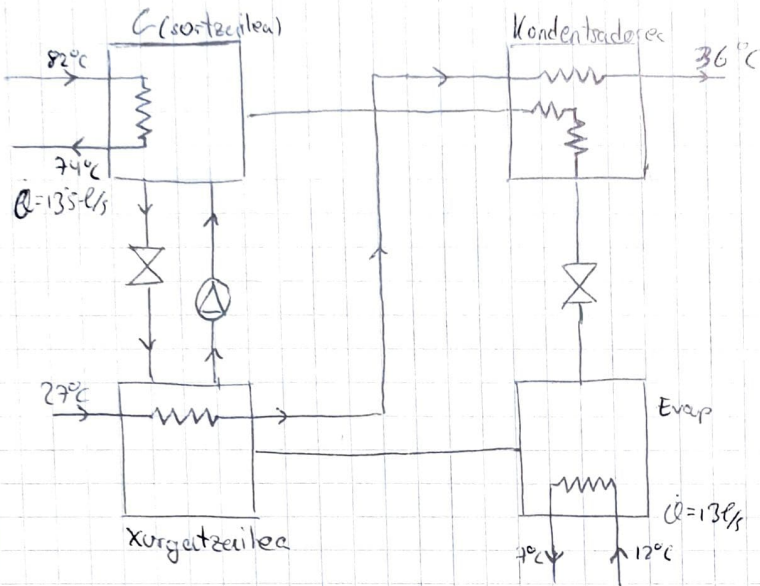
$$Q_{\text{gulerak}} = Q_{\text{karga}} - Q_{\text{deskarga}} = 12540 \text{ kJ}$$

$$Q_{\text{gulerak}} = \dot{m} \cdot C_p \cdot (T_{t_1} - T_{t_2}) \rightarrow T_{t_2} = 61 - \frac{12540}{3000 \cdot 4,18} \rightarrow T_{t_2} = 60^\circ\text{C}$$

$$\eta_1 = \%100 \quad \eta_2 = 1 - \frac{12540}{351120} = \%96,4 \quad \eta_3 = \%100 \rightarrow \eta_{\text{It}} = \%96,4$$

# Eguzki hozketa

Adibidea



$$\Delta E = Q - W = 0$$

$$Q_{evap} = \dot{m}_{evap} \cdot c_p \cdot \Delta T$$

$$Q_{evap} = 13 \cdot c_p \cdot (12 - 7)$$

$$Q_{evap} = 271.7 \text{ kW}$$

$$Q_c = \dot{m}_c \cdot c_p \cdot \Delta T$$

$$Q_c = 13.5 \cdot c_p \cdot (82 - 74) = 451.4 \text{ kW}$$

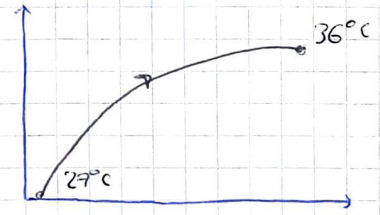
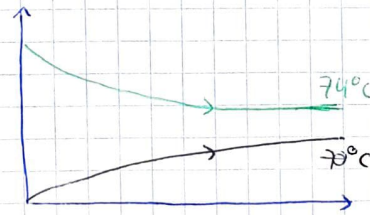
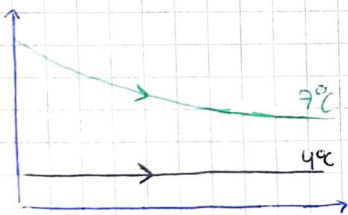
$$Q_{ref} = \dot{m}_{ref} \cdot c_p \cdot (36 - 7)$$

$$Q_c + Q_{evap} + W = Q_{ref} \rightarrow 451.4 + 271.7 = \dot{m}_{ref} \cdot 418 \cdot (9) \rightarrow \dot{m}_{ref} = 19.2 \text{ l/s}$$

$$EER = \frac{Q_{evap}}{Q_c} = \frac{271.7}{451.4} \rightarrow EER = 0.6$$

$$EER^{max} = \left(1 - \frac{T_m}{T_c}\right) \cdot \left(\frac{T_{evap}}{T_{evap} - T_{cond}}\right) \rightarrow EER^{max} = 0.63$$

Makina ona den etekin  
maximetik oso herbil deguziala



# Eguzki energia termikoa

## Eguzkia III

1) Palma de Mallorca:  $39^{\circ}34' \text{ I}$   $2^{\circ}39' \text{ E}$

Edimburgo:  $55^{\circ}57' \text{ I}$   $3^{\circ}10' \text{ M}$

Ekinetik 4 eta Abenduetik 4  $\rightarrow$  4/06  $\rightarrow \delta = +23^{\circ}27'$  // 4/12  $\rightarrow \delta = -23^{\circ}27'$

a) Eguzki irteera ordu ofiziale

Palma de Mallorca (4/06)

$$\cos \omega = \frac{+\sin(23^{\circ}27') \cdot \sin(39^{\circ}34')}{\cos(23^{\circ}27') \cdot \cos(39^{\circ}34')} = -\tan(23^{\circ}27') \cdot \tan(39^{\circ}34')$$

$$\omega = -110^{\circ}64'$$

$$\text{Eguzsenti ordua} = 12 - \frac{11064}{15} = 4^{\prime}62 = 4 \text{ ordu } 39 \text{ min } 26 \text{ s} \rightarrow \text{HSE-irupena !!}$$

$$\text{" " ofiziale} = \underline{6:37:26}$$

Palma de Mallorca (4/12)

$$\omega = \arccos(-\tan(-23^{\circ}27') \cdot \cos(39^{\circ}34')) = -69^{\circ}36'$$

$$\text{Eguzsenti ordu ofiziale} = 12 - \frac{6936}{15} + 1 = \underline{8:22:33}$$

Edimburgo (4/06)

$$\omega = \arccos(-\tan(23^{\circ}27') \cdot \tan(55^{\circ}57')) \rightarrow \omega = 178^{\circ}86'$$

$$\text{Eguzsenti ordu ofiziale} = 12 - \frac{17886}{15} + 1 = 4:24:34$$

Edimburgo (4/12)

$$\omega = \arccos(-\tan(-23^{\circ}27') \cdot \tan(55^{\circ}57')) \rightarrow \omega = -81^{\circ}14'$$

$$\text{Eguzsenti ordu ofiziale} = 12 - \frac{8114}{15} = 8:35:25$$

b) Eguziaren irupena

$$\text{Palma de Mallorca} \left\{ \begin{array}{l} 4/06 \rightarrow 2 \cdot 11064 \cdot \frac{1}{15} = 14^{\prime}75 \text{ h} \\ 4/12 \rightarrow 2 \cdot 6936 \cdot \frac{1}{15} = 9^{\prime}25 \text{ h} \end{array} \right.$$

$$\text{Edimburgo} \left\{ \begin{array}{l} 4/06 \rightarrow 2 \cdot 17886 \cdot \frac{1}{15} = 17^{\prime}18 \text{ h} \\ 4/12 \rightarrow 2 \cdot 8114 \cdot \frac{1}{15} = 6^{\prime}82 \text{ h} \end{array} \right.$$

c) ~~orbearen irupena~~  $\alpha$  eta  $\psi$ ? ordu ofiziale = 12h

Palma de Mallorca:

$$4/06 \rightarrow \text{OF: } 12\text{h} \rightarrow \text{HSE: } 10\text{h} \rightarrow \text{HSL} = 10 + 4(0 + 2^{\prime}65) + 2^{\prime}1 = 9:51:30 \text{ 10 ordu gehiago}$$

$$4/12 \rightarrow \text{OF: } 12\text{h} \rightarrow \text{HSE: } 11\text{h} \rightarrow \text{HSL} = 11 + 4(0 - 2^{\prime}65) + 4^{\prime}34 = 10^{\prime}98 \text{ h 11 ordu gutxiago}$$

$$4/06 \left\{ \begin{array}{l} \omega = 32^{\circ}25' \rightarrow \alpha = \arcsin(\sin(22^{\circ}34') \cdot \sin(39^{\circ}34') + \cos(22^{\circ}34') \cdot \cos(39^{\circ}34') \cdot \cos(32^{\circ}25')) \\ \alpha = 57^{\circ}86 \rightarrow \cos \psi = \frac{\sin(57^{\circ}86) \cdot \sin(39^{\circ}34) - \sin(22^{\circ}34)}{\cos(57^{\circ}86) \cdot \cos(39^{\circ}34)} \rightarrow \psi = 67^{\circ}62' \end{array} \right.$$

$$4/12 \left\{ \begin{array}{l} \omega = 15^{\circ}25' \rightarrow \alpha = \arcsin(\sin(-22^{\circ}14') \cdot \sin(39^{\circ}34') + \cos(-22^{\circ}14') \cdot \cos(39^{\circ}34') \cdot \cos(15^{\circ}25')) \\ \alpha = 26^{\circ}89 \rightarrow \cos \psi = \frac{\sin(26^{\circ}89) \cdot \sin(39^{\circ}34) - \sin(-22^{\circ}14)}{\cos(26^{\circ}89) \cdot \cos(39^{\circ}34)} \rightarrow \psi = 15^{\circ}84' \end{array} \right.$$

2) Apirilarren 18 →  $\delta = 9.84^\circ$ ,  $E_t = 0.02$

$\psi = 70^\circ \rightarrow \alpha = 0^\circ$

HSL = 12h → HSE = 11.44 → OF = 9.44

$\cos(\psi - \alpha) = \frac{\sin(\delta) \cdot \sin \phi - \sin(9.84)}{\cos(\delta) \cdot \cos \phi} \rightarrow \phi = 60.07^\circ$

$HSE = HSL - 4(L_s - L_c) - E_t$

$11.73 = 12 - 4(30 - L_c) - 0.02 \rightarrow L_c = -34^\circ E$

} Errusia

## Kolektorea II

1)  $\phi = 31.42' = 39.7^\circ$

$I = 6.82$

$\beta = 35^\circ$   $\psi = 0^\circ$

$I = 520 \frac{wh}{m^2} \cdot 1h \Rightarrow I = 520 \frac{wh}{m^2}$

Apirilarren 3a (10-11h)

$G_T = G_b \cdot R_b + G_a \cdot R_d + G \cdot f \cdot R_r$

$G = 520 \frac{wh}{m^2}$

$R_b = \frac{1 + \cos \beta}{2} = \frac{1 + \cos(35^\circ)}{2} = 0.91$

$f = 0.2$

$R_r = \frac{1 - \cos \beta}{2} = \frac{1 - \cos(\beta)}{2} = 0.09$

$\delta = 5.01^\circ$ ;  $E_t = -3.75$

$R_d = \frac{\cos \theta}{\sin \delta \cdot \sin \psi + \cos \delta \cdot \cos \phi \cdot \cos \psi}$

$R_d = \frac{\cos \theta}{\sin(5.01) \cdot \sin(39.42) + \cos(5.01) \cdot \cos(39.42) \cdot \cos(28.5)} =$

$k = \frac{G}{G_{on}} = \frac{520}{1371.64} \rightarrow k = 0.38$

$G_{on} = G_s \left( 1 + 0.033 \cdot \cos\left(\frac{360 \cdot \psi}{365}\right) \right) = 1373 \cdot \left( 1 + 0.033 \cdot \cos\left(\frac{360 \cdot 0}{365}\right) \right) \rightarrow G_{on} = 1371.64$

$\frac{G_p}{G} = 0.9511 - 0.1604k + 4.388k^2 - 16.678k^3 + 12.736k^4 \rightarrow \frac{G_p}{G} = 0.87$

## 2019-20 Geo orterket (Gaztelera)

Ariketa)

$$\text{Albacete: } \phi = 38^\circ \text{sq'}$$

$$12:00 \rightarrow \omega = 0^\circ$$

$$\text{Martxoak 3} \rightarrow 5/24 \text{ /d}$$

$$G_b = 1004 \text{ kW/m}^2$$

$$G_d = G \cdot 0.48$$

$$G = 1004 + G \cdot 0.48 \rightarrow G = \frac{1004}{1-0.48} \rightarrow G = 2004 \text{ kW/m}^2$$

$$G_T = G \cdot 0.9$$

$$PE \cdot R_r = 0.02 \cdot G_T \quad \left\{ \begin{array}{l} R_r = \frac{0.02 \cdot 2004 \cdot 0.9}{0.18 \cdot 2004} \rightarrow R_r = 0.1 \end{array} \right.$$

$$R_r = \frac{1 - \cos \beta}{2} \rightarrow \beta = 36.87^\circ$$

$$G_d \cdot R_d = G \cdot 0.48 \cdot \frac{1 + \cos \beta}{2} = 2004 \cdot 0.48 \cdot \frac{1 + \cos(36.87^\circ)}{2} \rightarrow G_d \cdot R_d = 0.903 \text{ kW/m}^2$$

## 2019-20 (Euskara)

Ariketa)

$$G_T = 1004 \text{ kW/m}^2 \quad \dot{m} = 1 \text{ l/s}$$

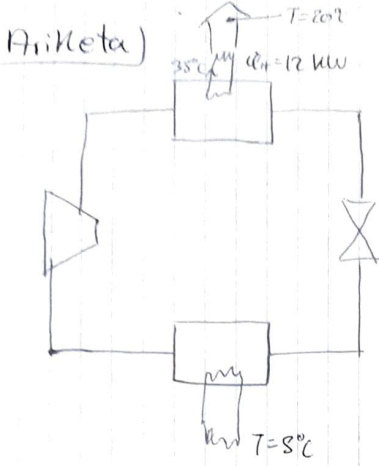
$$\alpha \cdot \tau = 0.95 \quad \text{10 totu}$$

$$p = 0.18$$

$$Q_c = G_T \cdot A_c \cdot \alpha \cdot \tau \cdot 0.1$$

$$Q_u = 0.1 \cdot G_T \cdot A_c \cdot \alpha \cdot \tau = \dot{m} \cdot C_p \cdot \Delta T \rightarrow \Delta T = \frac{0.1 \cdot 1004 \cdot 0.95}{0.1 \cdot 4.187} \rightarrow \Delta T =$$

# Energia geotermikou



$$COP = 3.2 = \frac{Q_H}{\dot{W}} = \frac{Q_H}{Q_H - Q_C}$$

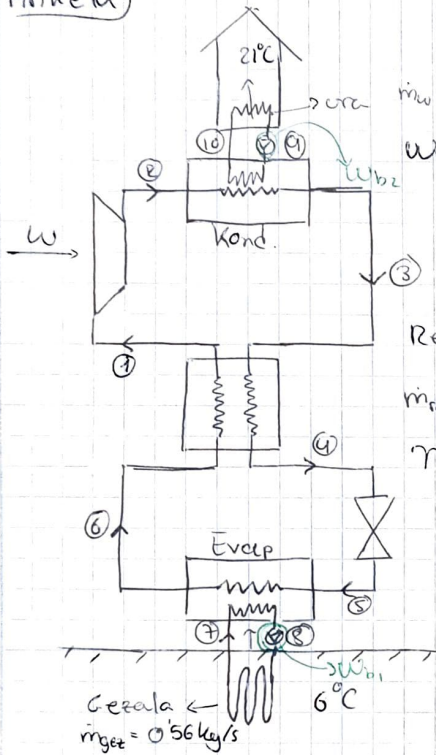
$$T_{00} = 0^\circ C$$

$$a) COP_{max} = \frac{T_H}{T_H - T_C} = \frac{283}{283 - 273} = 10.77$$

$$b) \dot{W} = \frac{Q_H}{3.2} = \frac{12}{3.2} = 3.75 \text{ kW}$$

$$c) \dot{W} = Q_H - Q_C \rightarrow Q_C = Q_H - \dot{W} = 12 - 3.75 = 8.25 \text{ kW}$$

Arkketa)



$$m_w = 0.28 \text{ kg/s}$$

$$W_{b2} = 60 \text{ W} \quad \eta_{b2} = 0.52$$

Refrig.

$$m_{ref} = 0.052 \text{ kg/s}$$

$$\eta_{comp} = 0.92$$

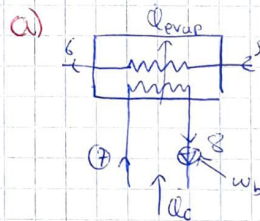
$$Q_{ref} = 9000 \text{ W}$$

Calderak

a)  $Q_C$ ?

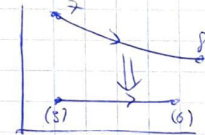
b) COP?

c)  $Q_{guterak}$ ?



$$Q_{evap} = \dot{m}_{ref} (h_8 - h_7) =$$

$$Q_{evap} = \dot{m}_{ref} (h_7 - h_8) = 5660 \text{ W}$$



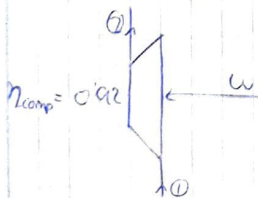
$$Q_c + Q_b = Q_{evap}$$

$$Q_c = Q_{evap} - Q_b = 5660 - 60 \cdot 0.52 = 5630 \text{ W}$$

$$b) COP = \frac{9000 \text{ W}}{W_{comp} + W_{b1} + W_{b2}} = \frac{9000}{3792 + 60 + 60} = 2.3$$

$$\eta_{comp} = \frac{\dot{m}_{ref} (h_2 - h_1)}{W_{comp}}$$

$$W_{comp} = \frac{\dot{m}_{ref} (h_2 - h_1)}{0.92} = 3792 \text{ W}$$



$$c) Q_{guterak} = Q_{goul}^{comp} + Q_{goul}^{b1} + Q_{goul}^{b2} - Q_{goul}^{evap} + Q_{goul}^{cond} + Q_{goul}^{bero-kerak} \rightarrow Q_{guterak} = 580.8 \text{ W}$$

$$Q_{goul}^{comp} = (1 - \eta_{comp}) W_{comp} = 303 \text{ W}$$

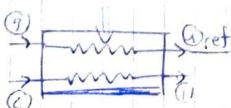
$$Q_{goul}^{b1} = (1 - \eta_{b1}) \cdot W_{b1} = 29 \text{ W}$$

$$Q_{goul}^{b2} = (1 - \eta_{b2}) \cdot W_{b2} = 29 \text{ W}$$

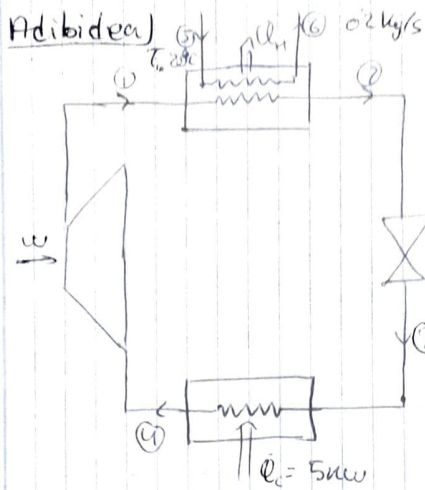
$$Q_{goul}^{evap} = \dot{m}_{ref} (h_7 - h_8) - \dot{m}_{ref} (h_6 - h_7) = -428 \text{ W}$$

$$Q_{goul}^{cond} = \dot{m}_{ref} (h_2 - h_3) - \dot{m}_w (h_6 - h_7) = 167 \text{ W}$$

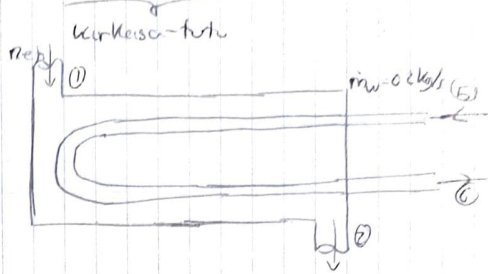
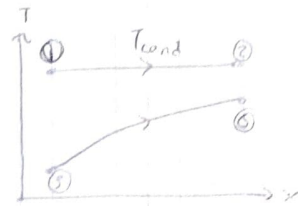
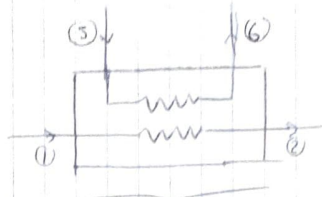
$$Q_{goul}^{bero-kerak} = \dot{m}_{ref} (h_2 - h_4) - \dot{m}_{ref} (h_1 - h_6) = 10 \text{ W}$$







$$COP = 2.5 - 0.01 (T_{cond} - 30)$$



$$h_{wf} = 11.3 \text{ W/m}^2\text{K}$$

$$h_{ref} = 10000 \text{ W/m}^2\text{K}$$

$$N = 50 \text{ tutku}$$

$$L = 3 \text{ m}$$

$$D_{in} = 0.02 \text{ m} \quad D_{out} = D_{in} + 2e$$

$$e = 0.001 \text{ m}$$

$$k = 15.1 \text{ W/mK}$$

2 eztegun daude

$$\Delta T_{ln} = \frac{(T_{cond} - T_5) - (T_{cond} - T_6)}{\ln \left( \frac{T_{cond} - T_5}{T_{cond} - T_6} \right)}$$

Calderak

a)  $T_{cond}$ ?

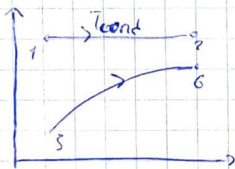
b)  $\dot{Q}_{cond}$ ?

$$COP = 2.5 - 0.01 (T_{cond} - 30) = \frac{\dot{Q}_c}{\dot{Q}_H - \dot{Q}_c}$$

$$\dot{Q}_H = UA \Delta T_{ln} = UA \cdot \left( \frac{\Delta T_{in} - \Delta T_{out}}{\ln \left( \frac{\Delta T_{in}}{\Delta T_{out}} \right)} \right)$$

$$\dot{Q}_{cond} = \dot{Q}_{ura}$$

$$\dot{Q}_{cond} = \dot{m}_{wg} \cdot \Delta h_{fg} \quad [ez dabilgu  $T_{cond}$  /  $P_{cond}$ ]$$



$$T_6 = T_{cond} - (T_{cond} - T_5) \cdot e^{-\frac{1}{k_{ext} \cdot m_{wg} \cdot c_p}}$$

$$\dot{Q}_{ura} = \dot{m}_{ura} \cdot c_p \cdot (T_{cond} - (T_{cond} - T_5) \cdot e^{-\frac{1}{k_{ext} \cdot m_{wg} \cdot c_p}} - T_5)$$

$$\dot{Q}_{ura} = \dot{m}_{ura} \cdot c_p \cdot (T_{cond} - T_5) \cdot (1 - e^{-\frac{1}{m_{wg} \cdot c_p \cdot k_{ext}}})$$

$$R_{Tot} = \frac{1}{h_{ref} \cdot A_{out}} + \frac{\ln \left( \frac{D_{out}}{D_{in}} \right)}{2\pi k L} + \frac{1}{h_{wf} \cdot A_{in}} = 9.646 \cdot 10^{-6} + 6.6972 \cdot 10^{-6} + 4.389 \cdot 10^{-4}$$

$$A_{out} = \pi \cdot D_{out} \cdot L \cdot N = 10.367 \text{ m}^2$$

$$A_{in} = \pi \cdot D_{in} \cdot L \cdot N = 9.425 \text{ m}^2$$