

TABLA

6

TRANSFORMADAS DE LAPLACE

	$f(s)$	$F(t)$
6.1	$\frac{1}{s}$	1
6.2	$\frac{1}{s^2}$	t
6.3	$\frac{1}{s^n} \quad n = 1, 2, 3, \dots$	$\frac{t^{n-1}}{(n-1)!}, \quad 0! = 1$
6.4	$\frac{1}{s^n} \quad n > 0$	$\frac{t^{n-1}}{\Gamma(n)}$
6.5	$\frac{1}{s-a}$	e^{at}
6.6	$\frac{1}{(s-a)^n} \quad n = 1, 2, 3, \dots$	$\frac{t^{n-1} e^{at}}{(n-1)!}, \quad 0! = 1$
6.7	$\frac{1}{(s-a)^n} \quad n > 0$	$\frac{t^{n-1} e^{at}}{\Gamma(n)}$
6.8	$\frac{1}{s^2 + a^2}$	$\frac{\sin at}{a}$
6.9	$\frac{s}{s^2 + a^2}$	$\cos at$
6.10	$\frac{1}{(s-b)^2 + a^2}$	$\frac{e^{bt} \sin at}{a}$
6.11	$\frac{s-b}{(s-b)^2 + a^2}$	$e^{bt} \cos at$
6.12	$\frac{1}{s^2 - a^2}$	$\frac{\sinh at}{a}$
6.13	$\frac{s}{s^2 - a^2}$	$\cosh at$

	$f(s)$	$F(t)$
6.14	$\frac{1}{(s - b)^2 - a^2}$	$\frac{e^{bt} \operatorname{senh} at}{a}$
6.15	$\frac{s - b}{(s - b)^2 - a^2}$	$e^{bt} \cosh at$
6.16	$\frac{1}{(s - a)(s - b)} \quad a \neq b$	$\frac{e^{bt} - e^{at}}{b - a}$
6.17	$\frac{s}{(s - a)(s - b)} \quad a \neq b$	$\frac{be^{bt} - ae^{at}}{b - a}$
6.18	$\frac{1}{(s^2 + a^2)^2}$	$\frac{\operatorname{sen} at - at \cos at}{2a^3}$
6.19	$\frac{s}{(s^2 + a^2)^2}$	$\frac{t \operatorname{sen} at}{2a}$
6.20	$\frac{s^2}{(s^2 + a^2)^2}$	$\frac{\operatorname{sen} at + at \cos at}{2a}$
6.21	$\frac{s^3}{(s^2 + a^2)^2}$	$\cos at - \frac{1}{2}at \operatorname{sen} at$
6.22	$\frac{s^2 - a^2}{(s^2 + a^2)^2}$	$t \cos at$
6.23	$\frac{1}{(s^2 - a^2)^2}$	$\frac{at \cosh at - \operatorname{senh} at}{2a^3}$
6.24	$\frac{s}{(s^2 - a^2)^2}$	$\frac{t \operatorname{senh} at}{2a}$
6.25	$\frac{s^2}{(s^2 - a^2)^2}$	$\frac{\operatorname{senh} at + at \cosh at}{2a}$
6.26	$\frac{s^3}{(s^2 - a^2)^2}$	$\cosh at + \frac{1}{2}at \operatorname{senh} at$
6.27	$\frac{s^2 + a^2}{(s^2 - a^2)^2}$	$t \cosh at$
6.28	$\frac{1}{(s^2 + a^2)^3}$	$\frac{(3 - a^2 t^2) \operatorname{sen} at - 3at \cos at}{8a^5}$

	$f(s)$	$F(t)$
6.29	$\frac{s}{(s^2 + a^2)^3}$	$\frac{t \sen at - at^2 \cos at}{8a^3}$
6.30	$\frac{s^2}{(s^2 + a^2)^3}$	$\frac{(1 + a^2 t^2) \sen at - at \cos at}{8a^3}$
6.31	$\frac{s^3}{(s^2 + a^2)^3}$	$\frac{3t \sen at + at^2 \cos at}{8a}$
6.32	$\frac{s^4}{(s^2 + a^2)^3}$	$\frac{(3 - a^2 t^2) \sen at + 5at \cos at}{8a}$
6.33	$\frac{s^5}{(s^2 + a^2)^3}$	$\frac{(8 - a^2 t^2) \cos at - 7at \sen at}{8}$
6.34	$\frac{3s^2 - a^2}{(s^2 + a^2)^3}$	$\frac{t^2 \sen at}{2a}$
6.35	$\frac{s^3 - 3a^2 s}{(s^2 + a^2)^3}$	$\frac{1}{2} t^2 \cos at$
6.36	$\frac{s^4 - 6a^2 s^2 + a^4}{(s^2 + a^2)^4}$	$\frac{1}{6} t^3 \cos at$
6.37	$\frac{s^3 - a^2 s}{(s^2 + a^2)^4}$	$\frac{t^3 \sen at}{24a}$
6.38	$\frac{1}{(s^2 - a^2)^3}$	$\frac{(3 + a^2 t^2) \senh at - 3at \cosh at}{8a^5}$
6.39	$\frac{s}{(s^2 - a^2)^3}$	$\frac{at^2 \cosh at - t \senh at}{8a^3}$
6.40	$\frac{s^2}{(s^2 - a^2)^3}$	$\frac{at \cosh at + (a^2 t^2 - 1) \senh at}{8a^3}$
6.41	$\frac{s^3}{(s^2 - a^2)^3}$	$\frac{3t \senh at + at^2 \cosh at}{8a}$
6.42	$\frac{s^4}{(s^2 - a^2)^3}$	$\frac{(3 + a^2 t^2) \senh at + 5at \cosh at}{8a}$
6.43	$\frac{s^5}{(s^2 - a^2)^3}$	$\frac{(8 + a^2 t^2) \cosh at + 7at \senh at}{8}$

	$f(s)$	$F(t)$
6.44	$\frac{3s^2 + a^2}{(s^2 - a^2)^3}$	$\frac{t^2 \operatorname{senh} at}{2a}$
6.45	$\frac{s^3 + 3a^2 s}{(s^2 - a^2)^3}$	$\frac{1}{2} t^2 \cosh at$
6.46	$\frac{s^4 + 6a^2 s^2 + a^4}{(s^2 - a^2)^4}$	$\frac{1}{6} t^3 \cosh at$
6.47	$\frac{s^3 + a^2 s}{(s^2 - a^2)^4}$	$\frac{t^3 \operatorname{senh} at}{24a}$
6.48	$\frac{1}{s^3 + a^3}$	$\frac{e^{at/2}}{3a^2} \left\{ \sqrt{3} \operatorname{sen} \frac{\sqrt{3} at}{2} - \cos \frac{\sqrt{3} at}{2} + e^{-3at/2} \right\}$
6.49	$\frac{s}{s^3 + a^3}$	$\frac{e^{at/2}}{3a} \left\{ \cos \frac{\sqrt{3} at}{2} + \sqrt{3} \operatorname{sen} \frac{\sqrt{3} at}{2} - e^{-3at/2} \right\}$
6.50	$\frac{s^2}{s^3 + a^3}$	$\frac{1}{3} \left(e^{-at} + 2e^{at/2} \cos \frac{\sqrt{3} at}{2} \right)$
6.51	$\frac{1}{s^3 - a^3}$	$\frac{e^{-at/2}}{3a^2} \left\{ e^{3at/2} - \cos \frac{\sqrt{3} at}{2} - \sqrt{3} \operatorname{sen} \frac{\sqrt{3} at}{2} \right\}$
6.52	$\frac{s}{s^3 - a^3}$	$\frac{e^{-at/2}}{3a} \left\{ \sqrt{3} \operatorname{sen} \frac{\sqrt{3} at}{2} - \cos \frac{\sqrt{3} at}{2} + e^{3at/2} \right\}$
6.53	$\frac{s^2}{s^3 - a^3}$	$\frac{1}{3} \left(e^{at} + 2e^{-at/2} \cos \frac{\sqrt{3} at}{2} \right)$
6.54	$\frac{1}{s^4 + 4a^4}$	$\frac{1}{4a^3} (\operatorname{sen} at \cosh at - \cos at \operatorname{senh} at)$
6.55	$\frac{s}{s^4 + 4a^4}$	$\frac{\operatorname{sen} at \operatorname{senh} at}{2a^2}$
6.56	$\frac{s^2}{s^4 + 4a^4}$	$\frac{1}{2a} (\operatorname{sen} at \cosh at + \cos at \operatorname{senh} at)$
6.57	$\frac{s^3}{s^4 + 4a^4}$	$\cos at \cosh at$
6.58	$\frac{1}{s^4 - a^4}$	$\frac{1}{2a^3} (\operatorname{senh} at - \operatorname{sen} at)$

	$f(s)$	$F(t)$
6.59	$\frac{s}{s^4 - a^4}$	$\frac{1}{2a^2} (\cosh at - \cos at)$
6.60	$\frac{s^2}{s^4 - a^4}$	$\frac{1}{2a} (\operatorname{senh} at + \operatorname{sen} at)$
6.61	$\frac{s^3}{s^4 - a^4}$	$\frac{1}{2} (\cosh at + \cos at)$
6.62	$\frac{1}{\sqrt{s+a} + \sqrt{s+b}}$	$\frac{e^{-bt} - e^{-at}}{2(b-a)\sqrt{\pi t^3}}$
6.63	$\frac{1}{s\sqrt{s+a}}$	$\frac{\operatorname{fer} \sqrt{at}}{\sqrt{a}}$
6.64	$\frac{1}{\sqrt{s(s-a)}}$	$\frac{e^{at} \operatorname{fer} \sqrt{at}}{\sqrt{a}}$
6.65	$\frac{1}{\sqrt{s-a+b}}$	$e^{at} \left\{ \frac{1}{\sqrt{\pi t}} - b e^{b^2 t} \operatorname{fcer} (b\sqrt{t}) \right\}$
6.66	$\frac{1}{\sqrt{s^2 + a^2}}$	$J_0(at)$
6.67	$\frac{1}{\sqrt{s^2 - a^2}}$	$I_0(at)$
6.68	$\frac{(\sqrt{s^2 + a^2} - s)^n}{\sqrt{s^2 + a^2}} \quad n > -1$	$a^n J_n(at)$
6.69	$\frac{(s - \sqrt{s^2 - a^2})^n}{\sqrt{s^2 - a^2}} \quad n > -1$	$a^n I_n(at)$
6.70	$\frac{e^{b(s-\sqrt{s^2+a^2})}}{\sqrt{s^2 + a^2}}$	$J_0(a\sqrt{t(t+2b)})$
6.71	$\frac{e^{-b\sqrt{s^2+a^2}}}{\sqrt{s^2 + a^2}}$	$\begin{cases} J_0(a\sqrt{t^2 - b^2}) & t > b \\ 0 & t < b \end{cases}$
6.72	$\frac{1}{(s^2 + a^2)^{3/2}}$	$\frac{t J_1(at)}{a}$

	$f(s)$	$F(t)$
6.73	$\frac{s}{(s^2 + a^2)^{3/2}}$	$tJ_0(at)$
6.74	$\frac{s^2}{(s^2 + a^2)^{3/2}}$	$J_0(at) - atJ_1(at)$
6.75	$\frac{1}{(s^2 - a^2)^{3/2}}$	$\frac{tI_1(at)}{a}$
6.76	$\frac{s}{(s^2 - a^2)^{3/2}}$	$tI_0(at)$
6.77	$\frac{s^2}{(s^2 - a^2)^{3/2}}$	$I_0(at) + atI_1(at)$
6.78	$\frac{1}{s(e^s - 1)} = \frac{e^{-s}}{s(1 - e^{-s})}$ Véase además 6.141.	$F(t) = n, n \leq t < n+1, n = 0, 1, 2, \dots$
6.79	$\frac{1}{s(e^s - r)} = \frac{e^{-s}}{s(1 - re^{-s})}$	$F(t) = \sum_{k=1}^{[t]} r^k$ donde $[t] = \text{máximo entero} \leq t$
6.80	$\frac{e^s - 1}{s(e^s - r)} = \frac{1 - e^{-s}}{s(1 - re^{-s})}$ Véase además 6.143.	$F(t) = r^n, n \leq t < n+1, n = 0, 1, 2, \dots$
6.81	$\frac{e^{-a/s}}{\sqrt{s}}$	$\frac{\cos 2\sqrt{at}}{\sqrt{\pi t}}$
6.82	$\frac{e^{-a/s}}{s^{3/2}}$	$\frac{\sin 2\sqrt{at}}{\sqrt{\pi a}}$
6.83	$\frac{e^{-a/s}}{s^{n+1}} \quad n > -1$	$\left(\frac{t}{a}\right)^{n/2} J_n(2\sqrt{at})$
6.84	$\frac{e^{-a\sqrt{s}}}{\sqrt{s}}$	$\frac{e^{-a^2/4t}}{\sqrt{\pi t}}$
6.85	$e^{-a\sqrt{s}}$	$\frac{a}{2\sqrt{\pi t^3}} e^{-a^2/4t}$

	$f(s)$	$F(t)$
6.86	$\frac{1 - e^{-a\sqrt{s}}}{s}$	$\text{fcer}(a/2\sqrt{t})$
6.87	$\frac{e^{-a\sqrt{s}}}{s}$	$\text{fcer}(a/2\sqrt{t})$
6.88	$\frac{e^{-a\sqrt{s}}}{\sqrt{s}(\sqrt{s} + b)}$	$e^{bt+a} \text{fcer}\left(b\sqrt{t} + \frac{a}{2\sqrt{t}}\right)$
6.89	$\frac{e^{-a/\sqrt{s}}}{s^{n+1}} \quad n > -1$	$\frac{1}{\sqrt{\pi t} a^{2n+1}} \int_0^\infty u^n e^{-u^2/4a^2t} J_{2n}(2\sqrt{u}) du$
6.90	$\ln\left(\frac{s+a}{s+b}\right)$	$\frac{e^{-bt} - e^{-at}}{t}$
6.91	$\frac{\ln[(s^2 + a^2)/a^2]}{2s}$	$Ic(at)$
6.92	$\frac{\ln[(s+a)/a]}{s}$	$Ie(at)$
6.93	$-\frac{(\gamma + \ln s)}{s}$ $\gamma = \text{constante de Euler} = 0,5772156\dots$	$\ln t$
6.94	$\ln\left(\frac{s^2 + a^2}{s^2 + b^2}\right)$	$\frac{2(\cos at - \cos bt)}{t}$
6.95	$\frac{\pi^2}{6s} + \frac{(\gamma + \ln s)^2}{s}$ $\gamma = \text{constante de Euler} = 0,5772156\dots$	$\ln^2 t$
6.96	$\frac{\ln s}{s}$	$-(\ln t + \gamma)$ $\gamma = \text{constante de Euler} = 0,5772156\dots$
6.97	$\frac{\ln^2 s}{s}$	$(\ln t + \gamma)^2 - \frac{1}{6}\pi^2$ $\gamma = \text{constante de Euler} = 0,5772156\dots$
6.98	$\frac{\Gamma'(n+1) - \Gamma(n+1)\ln s}{s^{n+1}} \quad n > -1$	$t^n \ln t$

	$f(s)$	$F(t)$
6.99	$\operatorname{tg}^{-1}(a/s)$	$\frac{\sin at}{t}$
6.100	$\frac{\operatorname{tg}^{-1}(a/s)}{s}$	$I_s(at)$
6.101	$\frac{e^{a/s}}{\sqrt{s}} \operatorname{fcer}(\sqrt{a/s})$	$\frac{e^{-2\sqrt{at}}}{\sqrt{\pi t}}$
6.102	$e^{s^2/4a^2} \operatorname{fcer}(s/2a)$	$\frac{2a}{\sqrt{\pi}} e^{-a^2t^2}$
6.103	$\frac{e^{s^2/4a^2} \operatorname{fcer}(s/2a)}{s}$	$\operatorname{fer}(at)$
6.104	$\frac{e^{as} \operatorname{fcer} \sqrt{as}}{\sqrt{s}}$	$\frac{1}{\sqrt{\pi(t+a)}}$
6.105	$e^{as} I_e(as)$	$\frac{1}{t+a}$
6.106	$\frac{1}{a} \left[\cos as \left\{ \frac{\pi}{2} - I_s(as) \right\} - \sin as I_c(as) \right]$	$\frac{1}{t^2 + a^2}$
6.107	$\sin as \left\{ \frac{\pi}{2} - I_s(as) \right\} + \cos as I_c(as)$	$\frac{t}{t^2 + a^2}$
6.108	$\frac{\cos as \left\{ \frac{\pi}{2} - I_s(as) \right\} - \sin as I_c(as)}{s}$	$\operatorname{tg}^{-1}(t/a)$
6.109	$\frac{\sin as \left\{ \frac{\pi}{2} - I_s(as) \right\} + \cos as I_c(as)}{s}$	$\frac{1}{2} \ln \left(\frac{t^2 + a^2}{a^2} \right)$
6.110	$\left[\frac{\pi}{2} - I_s(as) \right]^2 + I_c^2(as)$	$\frac{1}{t} \ln \left(\frac{t^2 + a^2}{a^2} \right)$
6.111	0	$\mathcal{N}(t) = \text{función nula}$
6.112	1	$\delta(t) = \text{función delta}$
6.113	e^{-as}	$\delta(t-a)$

	$f(s)$	$F(t)$
6.114	$\frac{e^{-as}}{s}$ Véase además 6.139.	$\mathcal{U}(t-a)$
6.115	$\frac{\operatorname{senh} sx}{s \operatorname{senh} sa}$	$\frac{x}{a} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \operatorname{sen} \frac{n\pi x}{a} \cos \frac{n\pi t}{a}$
6.116	$\frac{\operatorname{senh} sx}{s \cosh sa}$	$\frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{2n-1} \operatorname{sen} \frac{(2n-1)\pi x}{2a} \operatorname{sen} \frac{(2n-1)\pi t}{2a}$
6.117	$\frac{\cosh sx}{s \operatorname{senh} as}$	$\frac{t}{a} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \cos \frac{n\pi x}{a} \operatorname{sen} \frac{n\pi t}{a}$
6.118	$\frac{\cosh sx}{s \cosh sa}$	$1 + \frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{2n-1} \cos \frac{(2n-1)\pi x}{2a} \cos \frac{(2n-1)\pi t}{2a}$
6.119	$\frac{\operatorname{senh} sx}{s^2 \operatorname{senh} sa}$	$\frac{xt}{a} + \frac{2a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \operatorname{sen} \frac{n\pi x}{a} \operatorname{sen} \frac{n\pi t}{a}$
6.120	$\frac{\operatorname{senh} sx}{s^2 \cosh sa}$	$x + \frac{8a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^2} \operatorname{sen} \frac{(2n-1)\pi x}{2a} \cos \frac{(2n-1)\pi t}{2a}$
6.121	$\frac{\cosh sx}{s^2 \operatorname{senh} sa}$	$\frac{t^2}{2a} + \frac{2a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \cos \frac{n\pi x}{a} \left(1 - \cos \frac{n\pi t}{a}\right)$
6.122	$\frac{\cosh sx}{s^2 \cosh sa}$	$t + \frac{8a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^2} \cos \frac{(2n-1)\pi x}{2a} \operatorname{sen} \frac{(2n-1)\pi t}{2a}$
6.123	$\frac{\cosh sx}{s^3 \cosh sa}$	$\frac{1}{2}(t^2 + x^2 - a^2) - \frac{16a^2}{\pi^3} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^3} \cos \frac{(2n-1)\pi x}{2a} \cos \frac{(2n-1)\pi t}{2a}$
6.124	$\frac{\operatorname{senh} x \sqrt{s}}{\operatorname{senh} a \sqrt{s}}$	$\frac{2\pi}{a^2} \sum_{n=1}^{\infty} (-1)^n n e^{-n^2 \pi^2 t/a^2} \operatorname{sen} \frac{n\pi x}{a}$
6.125	$\frac{\cosh x \sqrt{s}}{\cosh a \sqrt{s}}$	$\frac{\pi}{a^2} \sum_{n=1}^{\infty} (-1)^{n-1} (2n-1) e^{-(2n-1)^2 \pi^2 t/4a^2} \cos \frac{(2n-1)\pi x}{2a}$
6.126	$\frac{\operatorname{senh} x \sqrt{s}}{\sqrt{s} \cosh a \sqrt{s}}$	$\frac{2}{a} \sum_{n=1}^{\infty} (-1)^{n-1} e^{-(2n-1)^2 \pi^2 t/4a^2} \operatorname{sen} \frac{(2n-1)\pi x}{2a}$
6.127	$\frac{\cosh x \sqrt{s}}{\sqrt{s} \operatorname{senh} a \sqrt{s}}$	$\frac{1}{a} + \frac{2}{a} \sum_{n=1}^{\infty} (-1)^n e^{-n^2 \pi^2 t/a^2} \cos \frac{n\pi x}{a}$

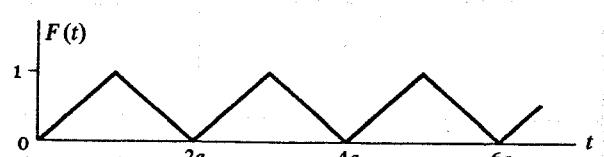
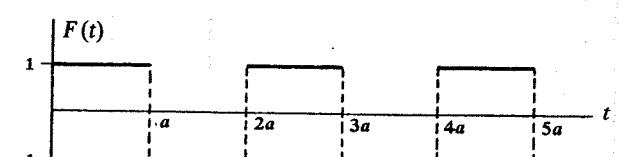
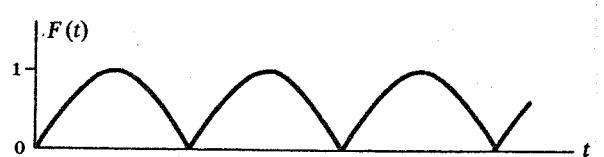
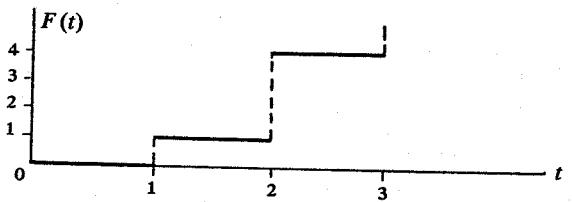
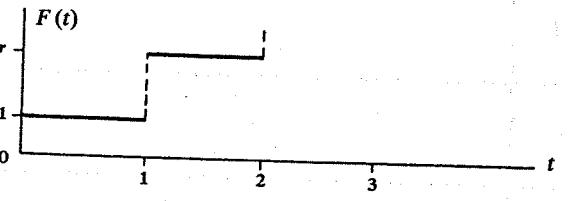
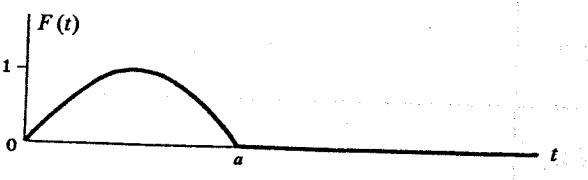
	$f(s)$	$F(t)$
6.128	$\frac{\operatorname{senh} x\sqrt{s}}{s \operatorname{senh} a\sqrt{s}}$	$\frac{x}{a} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} e^{-n^2\pi^2 t/a^2} \operatorname{sen} \frac{n\pi x}{a}$
6.129	$\frac{\cosh x\sqrt{s}}{s \cosh a\sqrt{s}}$	$1 + \frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{2n-1} e^{-(2n-1)^2\pi^2 t/4a^2} \cos \frac{(2n-1)\pi x}{2a}$
6.130	$\frac{\operatorname{senh} x\sqrt{s}}{s^2 \operatorname{senh} a\sqrt{s}}$	$\frac{xt}{a} + \frac{2a^2}{\pi^3} \sum_{n=1}^{\infty} \frac{(-1)^n}{n^3} (1 - e^{-n^2\pi^2 t/a^2}) \operatorname{sen} \frac{n\pi x}{a}$
6.131	$\frac{\cosh x\sqrt{s}}{s^2 \cosh a\sqrt{s}}$	$\frac{1}{2}(x^2 - a^2) + t - \frac{16a^2}{\pi^3} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^3} e^{-(2n-1)^2\pi^2 t/4a^2} \cos \frac{(2n-1)\pi x}{2a}$
6.132	$\frac{J_0(ix\sqrt{s})}{s J_0(i a\sqrt{s})}$	$1 - 2 \sum_{n=1}^{\infty} \frac{e^{-\lambda_n^2 t/a^2} J_0(\lambda_n x/a)}{\lambda_n J_1(\lambda_n)}$ donde $\lambda_1, \lambda_2, \dots$ son las raíces positivas de $J_0(\lambda) = 0$
6.133	$\frac{J_0(ix\sqrt{s})}{s^2 J_0(i a\sqrt{s})}$	$\frac{1}{4}(x^2 - a^2) + t + 2a^2 \sum_{n=1}^{\infty} \frac{e^{-\lambda_n^2 t/a^2} J_0(\lambda_n x/a)}{\lambda_n^3 J_1(\lambda_n)}$ donde $\lambda_1, \lambda_2, \dots$ son las raíces positivas de $J_0(\lambda) = 0$
6.134	$\frac{1}{as^2} \operatorname{tgh} \left(\frac{as}{2} \right)$	Función de onda triangular 
6.135	$\frac{1}{s} \operatorname{tgh} \left(\frac{as}{2} \right)$	Función de onda cuadrada 
6.136	$\frac{\pi a}{a^2 s^2 + \pi^2} \operatorname{cotgh} \left(\frac{as}{2} \right)$	Función de onda senoidal rectificada 

Fig. 6-3

	$f(s)$	$F(t)$
6.137	$\frac{\pi a}{(a^2 s^2 + \pi^2)(1 - e^{-as})}$	<p>Función de onda senoidal semi-rectificada</p>
6.138	$\frac{1}{as^2} - \frac{e^{-as}}{s(1 - e^{-as})}$	<p>Función de onda en diente de sierra</p>
6.139	$\frac{e^{-as}}{s}$ Véase además 6.114.	<p>Función unitaria de Heaviside $\mathcal{U}(t - a)$</p>
6.140	$\frac{e^{-as}(1 - e^{-es})}{s}$	<p>Función de pulsaciones</p>
6.141	$\frac{1}{s(1 - e^{-as})}$ Véase además 6.78.	<p>Función escalonada</p>

	$f(s)$	$F(t)$
6.142	$\frac{e^{-s} + e^{-2s}}{s(1 - e^{-s})^2}$	$F(t) = n^2, \quad n \leq t < n+1, \quad n = 0, 1, 2, \dots$  <p style="text-align: center;">Fig. 6-9</p>
6.143	$\frac{1 - e^{-s}}{s(1 - re^{-s})}$ Véase además 6.80.	$F(t) = r^n, \quad n \leq t < n+1, \quad n = 0, 1, 2, \dots$  <p style="text-align: center;">Fig. 6-10</p>
6.144	$\frac{\pi a(1 + e^{-as})}{a^2 s^2 + \pi^2}$	$F(t) = \begin{cases} \operatorname{sen}(\pi t/a) & 0 \leq t \leq a \\ 0 & t > a \end{cases}$  <p style="text-align: center;">Fig. 6-11</p>